

2.1 Coin and Mixture Problems

Be aware of the difference between
of coins and value of coins

# of coins	value of coins
3 dimes	$3(.10) = .30$
2 quarters	$2(.25) = .50$
5 nickels	$5(.05) = .25$
4 pennies	$4(.01) = .04$
x dimes	$x(.10) = .10x$
n quarters	$n(.25) = .25n$
m+3 nickels	$(m+3)(.05) = .05(m+3)$

Coin and Mixture Word Problems

1. Eleanor has \$1.60 in nickels and quarters. If there are 3 times as many quarters as nickels, how many of each type of coin does she have?

$$\begin{aligned}
 \text{let } x &= \# \text{ of nickels } (.05) \\
 3x &= \# \text{ of quarters } (.25) \\
 .05x + .25(3x) &= 1.60 \\
 .05x + .75x &= 1.60 \\
 .80x &= 1.60 \\
 x &= \frac{1.60}{.80} & 3x \\
 x &= 2 & 3(2) \\
 & & 6 \\
 & & 2 \text{ nickels and } 6 \text{ quarters}
 \end{aligned}$$

2. Bobby has 7 more nickels than dimes. He has \$1.55 in all. How many of each type of coin does he have?

$$\begin{aligned}
 \text{let } x &= \# \text{ of dimes } (.10) \\
 x+7 &= \# \text{ of nickels } (.05) \\
 .10(x) + .05(x+7) &= 1.55 \\
 .10x + .05(x) + .05(7) &= 1.55 \\
 .10x + .05x + .35 &= 1.55 \\
 .15x + .35 &= 1.55 \\
 .15x &= 1.55 - .35 \\
 .15x &= 1.20 & x+7 \\
 x &= \frac{1.20}{.15} & 8+7 \\
 & & 15 \\
 x &= 8 \\
 8 \text{ dimes and } 15 \text{ nickels}
 \end{aligned}$$

3. Hank has a collection of dimes and quarters worth \$4.50. He has 4 more quarters than dimes. Find the number of quarters.

$$\begin{aligned}
 \text{let } x &= \# \text{ of dimes } (.10) \\
 x+4 &= \# \text{ of quarters } (.25) \\
 .10(x) + .25(x+4) &= 4.50 \\
 .10x + .25x + 1.00 &= 4.50 \\
 .35x + 1.00 &= 4.50 \\
 .35x &= 4.50 - 1.00 \\
 .35x &= 3.50 & x+4 \\
 x &= \frac{3.50}{.35} & 10+4 \\
 & & 14 \\
 x &= 10 & 14 \text{ quarters}
 \end{aligned}$$

HOMEWORK

Worksheet - HW 2.1 - Coin & Mixture